

## Research Article

# Structural Efficiency of Non-Prismatic Reinforced Concrete Beams: A Comprehensive Review

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**ABSTRACT**

The use of non-prismatic reinforced concrete beams in construction and architecture has come as an innovative evolution to shape the future of structural design in relationship to construction material efficiency, economy, and versatility. Several structural, architectural, and economic advantages can be identified in the use of non-prismatic beams compared to conventional prismatic forms. In this review, distinct types of non-prismatic beams such as tapered, hunched, and segmented are presented, and their specific advantages and areas of applications in contemporary constructions, such as bridges and retrofitted infrastructures, are discussed. Alongside, highlights of advanced novel materials as well as design developments, such as glass and carbon fiber reinforced polymers or digital design technologies, which further enhance the structural, aesthetic, and sustainability performance of the non-prismatic components, are provided. Ultimately, challenges that non-prismatic beams currently face such as optimizing loads, enhancing cost-effectiveness, and reducing potentially excessive structural depth are discussed, as well as expectations for future developments in their design and applications. The potential of non-prismatic beams in providing a more sustainable, innovating, and contemporary evolution in construction practices is recognized.

**1. INTRODUCTION**

Non-prismatic reinforced concrete beams are structurally efficient and a major advancement in the evolution of construction and building practices. Their design, featuring a non-uniform cross-section, contrasts with the traditional prismatic beams with uniform cross-sectional properties. This allows for flexibility in designing for a wide range of engineering and architectural problems, making it useful in more applications than their prismatic counterparts. Non-prismatic beams can also be used to optimize material usage, particularly when specific load and performance criteria are needed for the structure. Furthermore, they are more commonly integrated into architectural designs, constructed not only for aesthetic purposes but also to satisfy certain specific structural requirements. In an age where the construction and building industry call for more efficient engineering and eco-friendly building solutions, there is a need to further research and understand non-prismatic reinforced concrete beams and how they can be designed, how they will behave under certain conditions [1-2].

This review paper aims to cover the comparative analysis of non-prismatic beams over the prismatic beams in discovering the structural performance and material efficiency of non-prismatic beams in achieving material optimization, cost efficiency, and sustainability through promising and innovative materials like fiber-reinforced polymers (FRP). This review paper intends to deal with the significant design approaches involving digital automation and performance-oriented methods alongside assessing the mechanical performance, load distribution, and environmental adaptability of non-prismatic beams. Moreover, this research paper also aims to include the practical utilization of non-prismatic beams in projects such as bridges, high-rise buildings, and retrofitting applications while addressing the prospective research requirements needed to promote non-prismatic beams in sustainable and eco-friendly construction practices.

**2. NON-PRISMATIC REINFORCED CONCRETE BEAMS**

The non-prismatic reinforced concrete beam is a structural member widely used in construction work. A Non-prismatic beam is a beam with varying cross-section dimensions along its length. It is different from a prismatic beam, which has a constant cross-section. The non-prismatic design of a beam involves the designing and formation of a beam with tapered

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or variable sections. In contrast to the prismatic beam, the non-prismatic design has some advantages, such as efficient usage of material, as prismatic beams may use excess material from design requirements. The design reduces the wastage of materials and money. The non-prismatic design is useful in buildings and architectural structures, especially in the formation of bridges, where a beam experiences a varying amount of stress along its length. The non-prismatic beam also helps in achieving good architectural features in buildings, which may be achieved through innovative approaches to use materials in achieving the desired looks. The outcome of a good non-prismatic design can lead to excellent architectural work and impact [3-4].

### 3. TYPES OF NON-PRISMATIC REINFORCED CONCRETE BEAMS

Understanding the type of prismatic beams makes it possible for an engineer to employ the method in a non-prismatic manner optimized to architectural and structural requirements for an enhanced overall value [5].

1. Tapered Beams: These have one or more slopes on their sides, with varying cross-section through the length of the beam. Commonly used in bridges and long span structures where load conditions vary through the span.
2. Haunched Beams: Increased depth at supports and reduced cross section at mid span, commonly used to counter increased bending moments near supports. Commonly practiced in frame structures and viaducts where support areas are subjected to more stresses.
3. Variable Depth Beams: Beams with constantly varying depth, suitable to optimize material distribution with respect to varying loading conditions. Applicable with structures having complex loading arrangements or where architectural requirements necessitate a change in the profile.
4. Segmented Beams: Consist of construction in segments with a combination of different cross-sections, commonly used in precast construction, tunnels and large span infrastructures like segmental bridges.

### 4. STRUCTURAL PROPERTIES OF NON-PRISMATIC BEAMS

Non-prismatic reinforced concrete beams, as the often being called variable depth beams, fall technological unique structural features as variable sections offer expected benefits in aspect of element performance and materials efficiency. Non-prismatic profiles entail beams that are non-uniform and being tapered in shapes, compared to prismatic which are usually having consistent cross-sectional areas along the length [6-7]. Such implied benefits due to effective load distributions along most of the length of the beam member not only provide an efficient solution by minimizing materials used in construction, but allow greater adaptability of the beams to specific demands and constraints of the structure itself. The mechanical performance of non-prismatic members may be further enhanced through use of corrugated steel webs therein. Such configuration allows greater depth of steel strands in balancing additional tensions and stability in demanding applications. These characteristics make non-prismatic beams particularly suitable for use in structures where aesthetic and functional requirements must be balanced, contributing to their growing popularity in modern construction.

The non-prismatic beams have a better load distribution and therefore have more advantages as compared to prismatic beams. Non-prismatic beams can accommodate variations in load, therefore improve the structural efficiency due to their varying cross-section [8]. A considerable advantage of a non-prismatic beam is that the structural design of choice for many complex architectural structures would give non-prismatic beams a leverage especially with varying loads. Also, the tapering of the non-prismatic beam design allows material reduction, potentially saving on costs without compromising on load-bearing capabilities [9]. With the load distributed efficiently and material usage optimized, there is a case for a non-prismatic beam as a preferred choice, aesthetically and structurally in construction today.

### 5. DESIGN CONSIDERATIONS

Non-prismatic beam design for reinforced concrete involves important considerations including geometry, material, and load bearing capacity. Geometry is the most important consideration since this determines the configuration of the beam. The configuration of the beam needs to be carefully determined to obtain the desired performance results including load-bearing capability [10]. Material is another key consideration in that this involves the selection of the right type of concrete and reinforcement. An appropriate material selection yields the desired performance results such as durability and strength [11]. The load bearing capacity is essential in determining whether the configuration can fit the specific demands of the construction projects [12]. All the aforementioned considerations play a significant role in determining the successful non-prismatic design of reinforced beams, with a proper implementation obtaining the desired results in terms of performance and aesthetics.

Several design methodologies can be applied to create non-prismatic beams, including their engineering principles that focus on their structural efficiency. One of the methodologies relates to performance-based design practices, in which specific constraints (that is, load-carrying capacity and material efficiency) are incorporated in the design processes of non-prismatic beams [13]. The latter can significantly increase the beams' durability and applicability, as they can be designed to carry specific loads and meet various environmental challenges. Another design methodology can be associated with the

digital design techniques that automate the beam geometry optimization process. Digital design automation enables precise material accommodation and effective construction processes, meeting various structural and aesthetic requirements [10]. Overall, the aforementioned design methodologies can be crucial in the creation of flexible and structurally efficient non-prismatic beams for various architectural needs and applications.

## 6. APPLICATIONS IN CONSTRUCTION

Non-prismatic reinforced concrete beam has found its way into the current building and construction industry, most notably with building designs that take advantage of the beam's tapered profile to improve its visual and structural performance. It serves prime architectural purposes in building designs, particularly those that require visually stunning elements along with functional utility such as public infrastructures and high-rise buildings [9]. One particular use of the non-prismatic design is found in bridges which benefit from its lighter weight and consequently requires less material usage to achieve the required strength [8]. Furthermore, the non-prismatic beam design can be found in retrofitting old structures to enhance a building's load-bearing characteristics without taking away from the original architectural design elements present in historical buildings [9]. These uses provide non-prismatic beams versatility in function as well as establishing it as a go-to design for buildings, both new and retrofitted.

It was pointed out in several case studies specific situations where non-prismatic beam design was successfully employed. One of the case studies focused on the usage of non-prismatic beams in bridge structures. Researchers concluded that tapered beam profiles allowed satisfying structural requirements, minimizing material usage without losing any load-bearing capacities [9]. Another approach highlighted in the case studies is related to the retrofitting of historical buildings with non-prismatic beams. Special care was taken to improve load-bearing characteristics while maintaining the initial appearance of a building [9]. Finally, non-prismatic beams can be found in high-rise architecture where beauty and load bearing coincide, offering a solution that satisfies both visual and functional aspects [12].

## 7. ADVANTAGES OVER PRISMATIC BEAMS

In comparison with traditional prismatic beams, non-prismatic beams have their own benefits and advantages. First of all, the geometry of non-prismatic beams provides superior distribution and use of materials. Consequently, it leads to lower material and cost usages [9]. At the same time, use of non-prismatic beams in buildings and structures effectively reduces the carbon footprint from concrete materials, which results in lower environmental impact [14]. The optimization of non-prismatic beams to different loading conditions also improves the overall performance of a structure, which has a positive effect during the whole service period and allows the building owner to save costs on maintenance and repair [12]. Therefore, non-prismatic beams can become an effective alternative and alternative solution for construction projects that require an economic balance between high-quality performance characteristics and environmental impacts.

One of the case studies discussed in this context about non-prismatic beams is with respect to their usage in the construction of a bridge. Non-prismatic beams in this case study were used to achieve load efficiency and consequently decrease the quantity of material consumption without compromising on the structural performance [9]. This allowed the overall performance of the bridge to improve further contributing to cost efficiency making a case for non-prismatic beams to be used in construction. Another case study discusses retrofitting of existing age-old buildings and using non-prismatic beams in order to increase load capacity without aesthetic loss of the buildings [12]. All of these case studies referenced are elaborative of the context of the usage of non-prismatic beams and how advantageous they can be in terms of the ratio between the beam material, overall performance, and structural efficiency.

## 8. ADVANCEMENTS IN MATERIALS

The most recent innovations in materials applied to non-prismatic reinforced concrete beams have focused on improving the applicability of this type of construction to meet modern-day structural and sustainability demands. The use of new composite materials, like fiber reinforced polymers (FRP) has been increasingly integrated to enhance the material properties of non-prismatic reinforced concrete beams [11]. Innovative applications of FRP systems to non-prismatic beams constructions have allowed more architectural designs to be realized by incorporating more complex geometries without compromising the structure's strength. These techniques for non-prismatic reinforced concrete beams have also aided the trend of implementing advanced retrofitting methods for existing constructions where carbon FRP sheets can be embedded into the concrete improving its load capacity [9]. Innovations of materials for non-prismatic reinforced concrete beam applications are vital for improving their role in contemporary construction moving forward.

In terms of the material developments for non-prismatic beams, the introduction of FRP (fiber-reinforced polymers) into the beams' systems has supported various improvements in overall performance and sustainability aspects. With FRP, non-prismatic beams have gained significant improvements in tensile capacity and durability, enabling complex and efficient designs that preserve structural performance across a wide range of situations [11]. In addition, CFRP (carbon fiber-reinforced polymer) sheets have been shown to be suitable for retrofitting works, supporting increased load-carrying

improvements and higher service life [9]. The development in materials is essential not only to support further reduce the impacts that these systems brought into the environment through reduced concrete consumptions, but also in overall building sustainability that continued to supporting the efficiency and sustainability [11]. In this regard, non-prismatic beams support further developments that will enable them to continue accommodate the demands of future construction practices, both in terms of the needs for innovative architecture and sustainable construction practices.

## 9. CONSTRUCTION TECHNIQUES

Construction techniques have played a crucial role in expediting the use of non-prismatic beams while also improving quality and safety. One of the notable construction techniques that improved the efficiency of construction processes and safety is digital design. With the aid of digital design technologies, it is possible to optimize the modeling of beam geometries before their actual construction [10]. The digital design enables precision placement of materials, thereby allowing for effective delivery of structural requirements while ensuring efficient use of material resources. In addition, prefabricated construction methods have resulted in reduced on-site construction labor requirements associated with non-prismatic construction materials, contributing to improved safety [11]. By reducing complex scaffolding and formwork, the prefabricated construction methods allow for quicker delivery times and consistent reliability of non-prismatic beams in architectural design. The non-prismatic beam architectural design improves project timelines through advancements in construction techniques. Digital design techniques allow for efficient modeling and optimization of beam geometries [10]. Digital design modeling enables precision delivery and conformity of structures, resulting in quicker project timelines and reduced time for adjustments on-site. Furthermore, prefabricated construction methodologies allow for quicker assembly of non-prismatic beams, reducing time on the construction site for scaffolding and formwork [11]. Traction timelines but also promote safer working conditions, contributing to the overall effectiveness and reliability of projects utilizing non-prismatic beam systems.

## 10. RESEARCH EVALUATION

The current literature available for non-prismatic reinforced concrete beams provide significant implications towards its application towards engineering design. One of the researches states that application of fiber-reinforced polymer (FRP) in-reinforced non-prismatic beam will enhance the mechanical properties and enables the detailed and complex beam design achieves structural integrity [11]. The performance-based design of non-prismatic beams can be applied on non-prismatic beams for enhanced earthquake strengthen [13]. Non-prismatic beams with corrugated steel webs create significant advantages for efficient loading and distribution as compared to the prismatic beams [8]. Therefore, further research should focus on optimizing the new design theory and materials to strengthen the application and explore the engineering design options that non-prismatic reinforced concrete beam offer.

Though there has been good progress in the studies related to non-prismatic beams in recent years, there are still some anomalies and gaps found in the literature. Some of these gaps can be seen in the performance studies done on the non-prismatic beams especially in extreme conditions such as earthquakes, fire, etc. It is important to evaluate and understand the performance of non-prismatic beams in such extreme conditions as it directly affects the serviceability and performance of the structure during the normal rainy season as well [15]. Another gap is that even though there are a number of studies stressing on the geometric and material benefits of the non-prismatic sections, there is minimal data found in the literature regarding the use of advanced material in non-prismatic beams such as fiber reinforced polymers (FRP) in tropical areas with varied environmental conditions [11]. Non-prismatic beams when used in large project constructions could save the project total budget. However, there is minimal data and analysis in the literature explaining the cost- potential savings by using non-prismatic beams [14]. These stats could also help increase the popularity of non-prismatic beams in the construction industry. Therefore, future studies should also target these gaps to better use the knowledge and expertise of non-prismatic beams.

## 11. CASE STUDY ANALYSIS

A recommended application of non-prismatic beams is in the case study of bridge construction, where their implementation improved load support as well as material usage. In this case study, it was found that the use of carbon fiber-reinforced polymer (CFRP) sheets on non-prismatic beams increased the structural functionality of beams while prolonging their service life is further lengthening bridge service life [9]. As for the construction phase, the engineered beams provided non-prismatic beams linearly changed cross-sections that allow easy implementation in site load specifications. Results showed reduced costs from construction due to lesser material usage, along with enhanced load-bearing and serviceability performance [12]. Overall, this case study demonstrates the efficacy of non-prismatic beams as a mainstream infrastructure beam for both cost and structural performance when enhanced by modern materials and construction technologies.

The future outlook of infrastructure projects, as per the case study of non-prismatic beams for bridge construction, involves strategic design and enhanced use of materials for optimal results against load and budget. More tailored designs based on

sight conditions using non-uniform cross-sections will produce desired outcomes only if complemented with precise engineering calculations [12]. However, the use of CFRP sheets in carbon fiber-reinforced polymer bridges yielded results for non-prismatic beams with better load-carrying capacity and service life. It drastically reduced initial and anticipated costs [9]. Using CFS and designing beams using materials and methods that promise more service life and stability will lead to more economic decisions with this type of beam.

## 12. FUTURE PROSPECTS

Non-prismatic reinforced concrete beams have a bright future in the construction industry due to the advancement of technology and demands for sustainable construction materials. With the advancement of digital design technologies, non-prismatic reinforced concrete beams allow engineers to design and analyze structural elements with high accuracy and speed, resulting in more efficient use of construction materials and energy [10]. In addition, advanced materials, such as fiber-reinforced polymers and self-healing concrete, have the potential to improve the performance and durability of non-prismatic reinforced concrete beams, making them more attractive for use in architectural masterpieces [11]. However, the existing challenges, such as cost-competitiveness and industry uptake, need to be resolved to ensure the wider use of non-prismatic reinforced concrete beams [14]. Ultimately, this will allow the non-prismatic design of reinforced concrete beams to significantly improve the sustainability of construction processes and promote creativity in architectural conceptualizations.

## 13. CONCLUSION

To sum up, non-prismatic reinforced concrete beams have become an important part of modern constructions because they provide improved structure flexibility and efficiency. The specific design of non-prismatic beams optimizes load distribution and material usage that implies both design and structural concerns for a variety of architectural projects. The advanced material application, in the form of fiber-reinforced polymers, has increased the mechanical properties of non-prismatic beams helping them to be utilized in complicated and sustainable constructions. The advancement in digital design and construction methods has improved implementation methods making them effective and safe. The construction industry-oriented work on sustainability and innovation will increase the importance of non-prismatic beams that will make them a common design for the future architectural and engineering practices.

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The authors declare no competing interests.

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